

## Chapter 4

## The Valuation of Long-Term Securities

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Created by: Gregory A. Kuhlemeyer, Ph.D.
Carroll College, Waukesha, WI


## After studying Chapter 4, you should be able to:

1. Distinguish among the various terms used to express value.
2. Value bonds, preferred stocks, and common stocks.
3. Calculate the rates of return (or yields) of different types of long-term securities.
4. List and explain a number of observations regarding the behavior of bond prices.


## The Valuation of Long-Term Securities

- Distinctions Among Valuation Concepts
- Bond Valuation
- Preferred Stock Valuation
- Common Stock Valuation
- Rates of Return (or Yields)


## What is Value?

-Liquidation value represents the amount of money that could be realized if an asset or group of assets is sold separately from its operating organization.

- Going-concern value represents the amount a firm could be sold for as a continuing operating business.


## What is Value?

-Book value represents either
(1) an asset: the accounting value of an asset -- the asset's cost minus its accumulated depreciation;
(2) a firm: total assets minus liabilities and preferred stock as listed on the balance sheet.

## What is Value?

- Market value represents the market price at which an asset trades.
$\bullet$ Intrinsic value represents the price a security "ought to have" based on all factors bearing on valuation.


## Bond Valuation

- Important Terms
- Types of Bonds
- Valuation of Bonds
- Handling Semiannual Compounding


## Important Bond Terms

- A bond is a long-term debt instrument issued by a corporation or government.
- The maturity value (MV) [or face value] of a bond is the stated value. In the case of a U.S. bond, the face value is usually $\mathbf{\$ 1 , 0 0 0}$.


## Important Bond Terms

- The bond's coupon rate is the stated rate of interest; the annual interest payment divided by the bond's face value.
- The discount rate (capitalization rate) is dependent on the risk of the bond and is composed of the risk-free rate plus a premium for risk.


## Different Types of Bonds

A perpetual bond is a bond that never matures. It has an infinite life.

$$
V=\frac{\|}{\left(1+k_{d}\right)^{1}}+\frac{\|}{\left(1+k_{\mathrm{d}}\right)^{2}}+\ldots+\frac{\|}{\left(1+k_{\mathrm{d}}\right)^{\infty}}
$$

$$
=\sum_{t=1}^{\infty} \frac{\|}{\left(1+k_{d}\right)^{t}} \quad \text { or } \quad l\left(\text { PVIFA }_{k_{d}, \infty}\right)
$$

$$
{ }_{4-16} \mathrm{~V}=\mathrm{I} / \mathrm{l} \mathrm{k}_{\mathrm{d}}
$$

[Reduced Form]

## Perpetual Bond Example

Bond $P$ has a \$1,000 face value and provides an 8\% annual coupon. The appropriate discount rate is $10 \%$. What is the value of the perpetual bond?

$$
\begin{aligned}
\mathrm{I} & =\$ 1,000(8 \%)=\$ 80 . \\
\mathrm{k}_{\mathrm{d}} & =10 \% . \\
\mathrm{V} & =\mathrm{I} / \mathrm{k}_{\mathrm{d}} \quad[\text { Reduced Form }] \\
& =\$ 80 / 10 \%=\$ 800 .
\end{aligned}
$$



## "Tricking" the Calculator to Solve

\section*{ | $\mathbf{N}$ | I/Y | PV | PMT | FV |
| :--- | :--- | :--- | :--- | :--- | <br> Compute}

N: "Trick" by using huge N like 1,000,000!
I/Y: 10\% interest rate per period (enter as 10 NOT .10)
PV: Compute (Resulting answer is cost to purchase)
PMT: \$80 annual interest forever ( $8 \% \times \$ 1,000$ face)
FV: $\quad \$ 0$ (investor never receives the face value)

## Different Types of Bonds

A non-zero coupon-paying bond is a coupon paying bond with a finite life.

$$
\begin{aligned}
V & =\frac{I}{\left(1+k_{d}\right)^{1}}+\frac{I}{\left(1+k_{d}\right)^{2}}+\ldots+\frac{I+M V}{\left(1+k_{d}\right)^{n}} \\
& =\sum_{t=1}^{n} \frac{I}{\left(1+k_{d}\right)^{n}}+\frac{M V}{\left(1+k_{d}\right)^{n}} \\
V & =I\left(\text { PVIFA }_{k_{d}, n}\right)+\text { MV }\left(\text { PVIF }_{k_{d}, n}\right)
\end{aligned}
$$

## Coupon Bond Example

Bond C has a \$1,000 face value and provides an $8 \%$ annual coupon for 30 years. The appropriate discount rate is $10 \%$. What is the value of the coupon bond?

```
\(\mathrm{V}=\$ 80\left(\right.\) PVIFA \(\left._{10 \%, 30}\right)+\$ 1,000\left(\right.\) PVIF \(\left._{10 \%, 30}\right)\)
                \(=\$ 80(9.427)+\$ 1,000(.057)\)
                [Table IV] [Table II]
= \$754.16 + \$57.00
= \$811.16.
```



## Solving the Coupon Bond on the Calculator

| Inputs | 30 | 10 |  | 80 | \$1,000 |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\mathbf{N}$ | I/Y | PV | PMT | FV |
| Compute |  | -811.46 |  | (Actual, rounding error in tables) |  |

N: 30-year annual bond
I/Y: 10\% interest rate per period (enter as 10 NOT .10)
PV: Compute (Resulting answer is cost to purchase)
PMT: \$80 annual interest ( $8 \% \times \$ 1,000$ face value)
FV: $\quad \$ 1,000$ (investor receives face value in 30 years)

## Different Types of Bonds

A zero coupon bond is a bond that pays no interest but sells at a deep discount from its face value; it provides compensation to investors in the form of price appreciation.

$$
V=\frac{M V}{\left(1+k_{d}\right)^{n}}=M V\left(P V I F_{k_{d}, n}\right)
$$



## Zero-Coupon Bond Example

Bond $Z$ has a $\$ 1,000$ face value and a 30 year life. The appropriate discount rate is $10 \%$. What is the value of the zero-coupon bond?

$$
\begin{aligned}
\mathrm{V} & =\$ 1,000\left(\mathrm{PVIF}_{10 \%}, 30\right) \\
& =\$ 1,000(.057) \\
& =\$ 57.00
\end{aligned}
$$



## Solving the Zero-Coupon Bond on the Calculator

| Inputs | 30 | 10 |  | 0 +\$1,000 |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\mathbf{N}$ | I/Y | PV | PMT | FV |
| Compute |  |  | -57.31 | (Actual error | unding <br> bles) |

N: 30-year zero-coupon bond
I/Y: 10\% interest rate per period (enter as 10 NOT .10)
PV: Compute (Resulting answer is cost to purchase)
PMT: \$0 coupon interest since it pays no coupon
FV: $\quad \$ 1,000$ (investor receives only face in $\mathbf{3 0}$ years)

## Semiannual Compounding

Most bonds in the U.S. pay interest twice a year (1/2 of the annual coupon).

Adjustments needed:
(1) Divide $k_{d}$ by 2
(2) Multiply $n$ by 2
(3) Divide I by 2

## Semiannual Compounding

## A non-zero coupon bond adjusted for semiannual compounding.

$$
\begin{aligned}
\mathrm{V} & =\frac{1 / 2}{\left(1+\sqrt{\left.k_{d} / 2\right)^{1}}\right)^{1}}+\frac{1 / 2}{\left(1+\mathrm{k}_{\mathrm{d}} / 2\right)^{2}}+\ldots+\frac{1 / 2+\mathrm{MV}}{\left(1+\mathrm{k}_{\mathrm{d}} / 2\right)^{2 * n}} \\
& =\sum_{\mathrm{t}=1}^{2^{*} n} \frac{1 / 2}{\left(1+\mathrm{k}_{\mathrm{d}} / 2\right)^{\mathrm{t}}}+\frac{\mathrm{MV}}{\left(1+\mathrm{k}_{\mathrm{d}} / 2\right)^{2 * n}} \\
& =1 / 2\left(\text { PVIFA }_{\mathrm{k}_{\mathrm{d}} / 2,2^{* n}}\right)+\mathrm{MV}\left(\text { PVIF }_{\mathrm{k}_{\mathrm{d}} / 2,2^{*} \mathrm{n}}\right)
\end{aligned}
$$

## Semiannual Coupon Bond Example

Bond C has a \$1,000 face value and provides an $8 \%$ semiannual coupon for 15 years. The appropriate discount rate is $10 \%$ (annual rate).

What is the value of the coupon bond?

$$
\begin{aligned}
\mathrm{V} \quad & =\$ 40\left(\mathrm{PVIFA}_{5 \%, 30}\right)+\$ 1,000\left(\text { PVIF }_{5 \%, 30}\right) \\
= & \$ 40(15,373)+\$ 1,000(.231) \\
& {[\text { Table IV] } \quad[\text { Table II }]} \\
= & \$ 614.92+\$ 231.00 \\
= & \$ 845.92
\end{aligned}
$$



## The Semiannual Coupon Bond on the Calculator

| Inputs | 30 | 5 |  | 40 +\$1,000 |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | N | I/Y | PV | PMT | FV |
| Compute |  |  | -846.28 | (Actual | unding |

N: 15-year semiannual coupon bond (15 x $2=30$ )
I/Y: $\quad 5 \%$ interest rate per semiannual period (10 / $2=5$ )
PV: Compute (Resulting answer is cost to purchase)
PMT: \$40 semiannual coupon (\$80 / 2 = \$40)
FV: $\quad \$ 1,000$ (investor receives face value in 15 years)

## Semiannual Coupon Bond Example

Let us use another worksheet on your calculator to solve this problem. Assume that Bond C was purchased (settlement date) on 12-31-2004 and will be redeemed on 12-31-2019. This is identical to the 15year period we discussed for Bond C.

What is its percent of par? What is the value of the bond?

## Solving the Bond Problem



## Press:

## $2^{\text {nd }}$

12.3104

ENTER

$\square$ ENTER

$\square$ ENTER


## 10

ENTER $\downarrow$


1. What is its percent of par?
2. What is the value of the bond?

- 84.628\% of par (as quoted in financial papers)
-84.628\% x \$1,000 face value $=\$ 846.28$


## Preferred Stock Valuation

Preferred Stock is a type of stock
that promises a (usually) fixed dividend, but at the discretion of the board of directors.

Preferred Stock has preference over common stock in the payment of dividends and claims on assets.

## Preferred Stock Valuation

$$
\begin{aligned}
V & =\frac{\operatorname{Div}_{P}}{\left(1+k_{P}\right)^{1}}+\frac{\operatorname{Div}_{P}}{\left(1+k_{P}\right)^{2}}+\ldots+\frac{\text { Div }_{P}}{\left(1+k_{P}\right)^{\infty}} \\
& =\sum_{t=1}^{\infty} \frac{\text { Div }_{P}}{\left(1+k_{P}\right)^{t}} \quad \text { or } \operatorname{Div}_{P}\left(\text { PVIFA }_{k_{p}, \infty}\right)
\end{aligned}
$$

## This reduces to a perpetuity!

$$
\mathrm{V}=\operatorname{Div}_{\mathrm{p}} / \mathrm{k}_{\mathrm{p}}
$$

## Preferred Stock Example

Stock PS has an 8\%, \$100 par value issue outstanding. The appropriate discount rate is $10 \%$. What is the value of the preferred stock?

$$
\begin{array}{ll}
\operatorname{Div}_{\mathrm{P}} & =\$ 100(8 \%)=\$ 8.00 \\
\mathrm{k}_{\mathrm{p}} & =10 \% . \\
\mathrm{V} & =\operatorname{Div}_{\mathrm{p}} / \mathrm{k}_{\mathrm{p}}=\$ 8.00 / 10 \% \\
& =\$ 80
\end{array}
$$

## Common Stock Valuation

Common stock represents a residual ownership position in the corporation.

- Pro rata share of future earnings after all other obligations of the firm (if any remain).
- Dividends may be paid out of the pro rata share of earnings.


## Common Stock Valuation

## What cash flows will a shareholder receive when owning shares of common stock?

(1) Future dividends
(2) Future sale of the common stock shares

## Dividend Valuation Model

Basic dividend valuation model accounts for the PV of all future dividends.

$$
\begin{aligned}
V & =\frac{\text { Div }_{1}}{\left(1+k_{e}\right)^{1}}+\frac{\text { Div }_{2}}{\left(1+k_{e}\right)^{2}}+\ldots+\frac{\text { Div }_{\infty}}{\left(1+k_{e}\right)^{\infty}} \\
& =\sum_{t=1}^{\infty} \frac{\text { Div }_{t}}{\left(1+k_{e}\right)^{t}} \quad \begin{array}{ll}
\text { Div }_{t}: \begin{array}{l}
\text { Cash Dividend } \\
\text { at time } t
\end{array} \\
k_{e}: \begin{array}{l}
\text { Equity investor's } \\
\text { required return }
\end{array}
\end{array}
\end{aligned}
$$



## Adjusted Dividend Valuation Model

The basic dividend valuation model adjusted for the future stock sale.

$$
\mathrm{V}=\frac{\text { Div }_{1}}{\left(1+k_{e}\right)^{1}}+\frac{\text { Div }_{2}}{\left(1+k_{e}\right)^{2}}+\ldots+\frac{\text { Div }_{n}+\text { Price }_{n}}{\left(1+k_{e}\right)^{n}}
$$

The year in which the firm's shares are expected to be sold.
Price $n$ : The expected share price in year $n$.


## Dividend Growth Pattern Assumptions

The dividend valuation model requires the forecast of all future dividends. The
following dividend growth rate assumptions simplify the valuation process.

Constant Growth

## No Growth

Growth Phases

## Constant Growth Model

## The constant growth model assumes that dividends will grow forever at the rate $g$.

$$
V=\frac{D_{0}(1+g)}{\left(1+k_{e}\right)^{1}}+\frac{D_{0}(1+g)^{2}}{\left(1+k_{e}\right)^{2}}+\ldots+\frac{D_{0}(1+g)^{\infty}}{\left(1+k_{e}\right)^{\infty}}
$$


$\mathrm{D}_{1}$ : $\quad$ Dividend paid at time 1.
g: The constant growth rate.
$k_{e}$ : Investor's required return.


## Constant Growth Model Example

Stock CG has an expected dividend growth rate of 8\%. Each share of stock just received an annual $\$ 3.24$ dividend. The appropriate discount rate is $15 \%$. What is the value of the common stock?
$\mathrm{D}_{1}=\$ 3.24(1+.08)=\$ 3.50$
$V_{C G}=D_{1} I\left(k_{e}-g\right)=\$ 3.50 /(.15-.08)$
= \$50

## Zero Growth Model

The zero growth model assumes that dividends will grow forever at the rate $\mathrm{g}=0$.

$$
V_{z G}=\frac{D_{1}}{\left(1+k_{e}\right)^{1}}+\frac{D_{2}}{\left(1+k_{e}\right)^{2}}+\ldots+\frac{D_{\infty}}{\left(1+k_{e}\right)^{\infty}}
$$


$\mathrm{D}_{1}$ : Dividend paid at time 1.
$\mathrm{k}_{\mathrm{e}}$ : Investor's required return.

## Zero Growth Model Example

Stock ZG has an expected growth rate of 0\%. Each share of stock just received an annual $\$ 3.24$ dividend per share. The appropriate discount rate is 15\%. What is the value of the common stock?

$$
\begin{aligned}
\mathrm{D}_{1} & =\$ 3.24(1+0)=\$ 3.24 \\
\mathrm{~V}_{\mathrm{ZG}} & =\mathrm{D}_{1} I\left(\mathrm{k}_{\mathrm{e}}-0\right)=\$ 3.24 /(.15-0) \\
& =\$ 21.60
\end{aligned}
$$

## Growth Phases Model

The growth phases model assumes that dividends for each share will grow at two or more different growth rates.

$$
\mathbf{V}=\sum_{t=1}^{n} \frac{D_{0}\left(1+g_{1}\right)^{t}}{\left(1+k_{e}\right)^{t}}+\sum_{t=n+1}^{\infty} \frac{D_{n}\left(1+g_{2}\right)^{t}}{\left(1+k_{e}\right)^{t}}
$$

## Growth Phases Model

Note that the second phase of the growth phases model assumes that dividends will grow at a constant rate $g_{2}$. We can rewrite the formula as:

$$
\mathbf{V}=\sum_{t=1}^{n} \frac{D_{0}\left(1+g_{1}\right)^{t}}{\left(1+k_{e}\right)^{t}}+\left[\frac{1}{\left(1+k_{e}\right)}\right]\left[\frac{D_{n+1}}{\left(k_{e}-g_{2}\right)}\right]
$$



## Growth Phases Model Example

Stock GP has an expected growth rate of $16 \%$ for the first 3 years and 8\% thereafter. Each share of stock just received an annual \$3.24 dividend per share. The appropriate discount rate is $15 \%$. What is the value of the common stock under this scenario?


## Growth Phases Model Example



Stock GP has two phases of growth. The first, 16\%, starts at time $\mathbf{t}=0$ for 3 years and is followed by $8 \%$ thereafter starting at time $t=3$. We should view the time line as two separate time lines in the valuation.

## Growth Phases Model Example



Note that we can value Phase \#2 using the Constant Growth Model


## Growth Phases Model Example

## $\mathrm{V}_{3}=\frac{\mathrm{D}_{4}}{\mathrm{k}-\mathrm{g}}$

We can use this model because dividends grow at a constant 8\% rate beginning at the end of Year 3.


Note that we can now replace all dividends from year 4 to infinity with the value at time $t=3, V_{3}$ ! Simpler!!

## Growth Phases Model Example



Now we only need to find the first four dividends to calculate the necessary cash flows.


## Growth Phases Model Example

## Determine the annual dividends.

$D_{0}=\$ 3.24$ (this has been paid already) $^{D_{1}=D_{0}\left(1+g_{1}\right)^{1}=\$ 3.24(1.16)^{1}=\$ 3.76}$
$D_{2}=D_{0}\left(1+g_{1}\right)^{2}=\$ 3.24(1.16)^{2}=\$ 4.36$
$D_{3}=D_{0}\left(1+g_{1}\right)^{3}=\$ 3.24(1.16)^{3}=\$ 5.06$
$D_{4}=D_{3}\left(1+g_{2}\right)^{1}=\$ 5.06(1.08)^{1}=\$ 5.46$

## Growth Phases Model Example



Now we need to find the present value of the cash flows.


## Growth Phases Model Example

We determine the PV of cash flows.

$$
\begin{gathered}
\operatorname{PV}\left(D_{1}\right)=D_{1}\left(\mathrm{PVIF}_{15 \%, 1}\right)=\$ 3.76(.870)=\$ \underline{3.27} \\
\operatorname{PV}\left(D_{2}\right)=D_{2}\left(\mathrm{PVIF}_{15 \%, 2}\right)=\$ 4.36(.756)=\$ \underline{3.30} \\
\operatorname{PV}\left(D_{3}\right)=D_{3}\left(\operatorname{PVIF}_{15 \%, 3}\right)=\$ 5.06(.658)=\$ \underline{3.33} \\
P_{3}=\$ 5.46 \text { I }(.15-.08)=\$ 78 \text { [CG Model] }
\end{gathered}
$$

$$
\operatorname{PV}\left(P_{3}\right)=P_{3}\left(\mathrm{PVIF}_{15 \%, 3}\right)=\$ 78(.658)=\$ 51.32
$$



## Growth Phases Model Example

Finally, we calculate the intrinsic value by summing all of cash flow present values.



## Solving the Intrinsic Value Problem using CF Registry

Steps in the Process (Page 1)



## Solving the Intrinsic Value Problem using CF Registry

Steps in the Process (Page 2)

| Step 8: For C03 Press | 83.06 | Enter | keys |
| :---: | :---: | :---: | :---: |
| Step 9: For F03 Press | 1 | Enter | keys |
| Step 10: Press | $\downarrow$ | $\downarrow$ | keys |
| Step 11: Press | NPV |  |  |
| Step 12: Press | 15 | Enter $\downarrow$ | keys |
| Step 13: Press | CPT |  |  |

RESULT: Value $=\mathbf{\$ 6 1 . 1 8 !}$
(Actual - rounding error in tables)


## Calculating Rates of Return (or Yields)

## Steps to calculate the rate of

 return (or Yield).1. Determine the expected cash flows.
2. Replace the intrinsic value ( V ) with the market price ( $\mathrm{P}_{0}$ ).
3. Solve for the market required rate of return that equates the discounted cash flows to the market price.

## Determining Bond YTM

## Determine the Yield-to-Maturity (YTM) for the annual coupon paying bond with a finite life.

$$
\begin{aligned}
P_{0} & =\sum_{t=1}^{n} \frac{I}{\left(1+\sqrt{k_{d}}\right)^{t}}+\frac{M V}{(1+\sqrt[k_{d}]{ })^{n}} \\
& \left.=I\left(\text { PVIFA }{ }_{k_{d}}, n\right)+\text { MV (PVIF }{ }_{\left[k_{d}\right.}, n\right) \\
k_{d} & =\text { YTM }
\end{aligned}
$$

## Determining the YTM

Julie Miller want to determine the YTM for an issue of outstanding bonds at Basket Wonders (BW). BW has an issue of 10\% annual coupon bonds with 15 years left to maturity. The bonds have a current market value of $\$ 1,250$.

What is the YTM?

## YTM Solution (Try 9\%)

$$
\begin{aligned}
& \$ 1,250= \begin{array}{l}
\$ 100\left(\text { PVIFA }_{9 \%, 15}\right)+ \\
\\
\$ 1,000\left(\mathrm{PVIF}_{9 \%, 15}\right)
\end{array} \\
& \$ 1,250=\begin{array}{l}
\$ 100(8.061)+ \\
\$ 1,000(.275)
\end{array},
\end{aligned}
$$

$\$ 1,250=\$ 806.10+\$ 275.00$
$\neq \$ 1,081.10$
[Rate is too high!]

## YTM Solution (Try 7\%)

$\mathbf{\$ 1 , 2 5 0}=\$ 100\left(\right.$ PVIFA $\left._{7 \%, 15}\right)+$ \$1,000(PVIF ${ }_{7 \%, 15}$ )
$\$ 1,250=\$ 100(9.108)+$ \$1,000(.362)
\$1,250 = \$910.80 + \$362.00
$\neq \$ 1,272.80$ [Rate is too low!]

## YTM Solution (Interpolate)

$$
\begin{aligned}
& .02\left[\begin{array}{c}
\times\left[\begin{array}{cc}
.07 & \$ 1,273 \\
\operatorname{IRR} & \$ 1,250
\end{array}\right] \$ 23 \\
.09 \$ 1,081
\end{array}\right] \$ 192 \\
& \frac{x}{.02}=\frac{\$ 23}{\$ 192}
\end{aligned}
$$

## YTM Solution (Interpolate)

$.02\left[\begin{array}{cc}\times\left[\begin{array}{cc}.07 & \$ 1,273 \\ \operatorname{RR} & \$ 1,250\end{array}\right] \$ 23 \\ .09 & \$ 1,081\end{array}\right] \$ 192$
$\frac{x}{.02}=\frac{\$ 23}{\$ 192}$

## YTM Solution (Interpolate)

$$
.02\left[\begin{array}{ccc}
\times\left[\begin{array}{ccc}
.07 & \$ 1273 & \\
\text { YTM } & \$ 1250
\end{array}\right] \$ 23 \\
.09 & \$ 1081
\end{array}\right] \$ 192
$$

$$
X=\frac{(\$ 23)(0.02)}{\$ 192} \quad X=.0024
$$

$\mathrm{YTM}=.07+.0024=.0724$ or $7.24 \%$


## YTM Solution on the Calculator

| Inputs | 15 | -1,250 |  | 100 | +\$1,000 |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | N | I/Y | PV | PMT | FV |
| Compute |  | 7.22\% | actua | YTM) |  |

N: 15-year annual bond
I/Y: Compute -- Solving for the annual YTM
PV: Cost to purchase is $\mathbf{\$ 1 , 2 5 0}$
PMT: \$100 annual interest ( $10 \% \times \mathbf{1 , 0 0 0}$ face value)
FV: $\quad \$ 1,000$ (investor receives face value in 15 years)

# Determining Semiannual Coupon Bond YTM 

## Determine the Yield-to-Maturity (YTM) for the semiannual coupon paying bond with a finite life.

$$
\begin{aligned}
P_{0} & =\sum_{t=1}^{2 n} \frac{1 / 2}{\left(1+\left[\underline{k d}_{d} / 2\right)^{)^{2}}\right.}+\frac{M V}{\left(1+\left[{\left.\underline{k_{d}} / 2\right)^{2 n}}^{2}\right.\right.} \\
& =(1 / 2)\left(\text { PVIFA }_{k_{d}} / 2,2 n\right)+M V\left(\text { PVIF }_{k_{d} / 2,2 n}\right) \\
& {\left[1+\left(k_{d} / 2\right)^{2}\right]-1=\text { YTM } }
\end{aligned}
$$



## Determining the Semiannual Coupon Bond YTM

Julie Miller want to determine the YTM for another issue of outstanding bonds. The firm has an issue of 8\% semiannual coupon bonds with 20 years left to maturity. The bonds have a current market value of $\$ 950$.
What is the YTM?


## YTM Solution on the Calculator



N: 20-year semiannual bond (20 x $2=40$ )
I/Y: Compute -- Solving for the semiannual yield now
PV: Cost to purchase is $\$ 950$ today
PMT: \$40 annual interest ( $8 \% \times \$ 1,000$ face value / 2)
FV: $\quad \$ 1,000$ (investor receives face value in 15 years)

# Determining Semiannual Coupon Bond YTM 

## Determine the Yield-to-Maturity (YTM) for the semiannual coupon paying bond with a finite life.

$$
\left[1+\left(k_{d} / 2\right)^{2}\right]-1=\text { YTM }
$$

$$
\begin{gathered}
{\left[1+(.042626)^{2}\right]-1=.0871} \\
\text { or } 8.71 \%
\end{gathered}
$$

## Solving the Bond Problem

## 㙁 Texas Instruments <br> 



## Press:

## $2^{\text {nd }}$ <br> Bond <br> 12.3104 <br> ENTER <br> 


ENTER $\downarrow$ 12.3124 ENTER $\downarrow$


| $\mathbf{9 5}$ |
| :---: |
| CPT |



# Determining Semiannual Coupon Bond YTM 

This technique will calculate $\mathrm{k}_{\mathrm{d}}$. You must then substitute it into the following formula.

$$
\left[1+\left(k_{d} / 2\right)^{2}\right]-1=\text { YTM }
$$

[ 1 + (.0852514/2) ${ }^{2}$ ]-1 = . 0871 or 8.71\% (same result!)


## Bond Price - Yield Relationship

Discount Bond -- The market required rate of return exceeds the coupon rate (Par $>\mathrm{P}_{0}$ ).
Premium Bond -- The coupon rate exceeds the market required rate of return ( $\mathrm{P}_{0}>\mathrm{Par}$ ).
Par Bond -- The coupon rate equals the market required rate of return ( $\mathrm{P}_{0}=\mathrm{Par}$ ). 4-66


## Bond Price - Yield Relationship



MARKET REQUIRED RATE OF RETURN (\%)


## Bond Price-Yield Relationship

## When interest rates rise, then the market required rates of return rise and bond prices will fall.

Assume that the required rate of return on a 15 year, $10 \%$ annual coupon paying bond rises from $10 \%$ to $12 \%$. What happens to the bond price?



MARKET REQUIRED RATE OF RETURN (\%)


## Bond Price-Yield Relationship (Rising Rates)

The required rate of return on a 15 year, 10\% annual coupon paying bond has risen from $10 \%$ to $12 \%$.

Therefore, the bond price has fallen from \$1,000 to \$864.
(\$863.78 on calculator)


## Bond Price-Yield Relationship

# When interest rates fall, then the market required rates of return fall and bond prices will rise. 

Assume that the required rate of return on a 15 year, 10\% annual coupon paying bond falls from $10 \%$ to 8\%. What happens to the bond price?



MARKET REQUIRED RATE OF RETURN (\%)

## Bond Price-Yield Relationship (Declining Rates)

# The required rate of return on a 15 year, $10 \%$ coupon paying bond has fallen from 10\% to 8\%. 

Therefore, the bond price has risen from \$1000 to \$1171.
(\$1,171.19 on calculator)

## The Role of Bond Maturity

The longer the bond maturity, the greater the change in bond price for a given change in the market required rate of return.

Assume that the required rate of return on both the 5 and 15 year, 10\% annual coupon paying bonds fall from 10\% to 8\%. What happens to the changes in bond prices?



MARKET REQUIRED RATE OF RETURN (\%)

## The Role of Bond Maturity

The required rate of return on both the 5 and 15 year, $10 \%$ annual coupon paying bonds has fallen from 10\% to 8\%.

The 5 year bond price has risen from \$1,000 to \$1,080 for the 5 year bond (+8.0\%).
The 15 year bond price has risen from \$1,000 to \$1,171 (+17.1\%). Twice as fast!


## The Role of the Coupon Rate

## For a given change in the

 market required rate of return, the price of a bond will change by proportionally more, the lower the coupon rate.

## Example of the Role of the Coupon Rate

Assume that the market required rate of return on two equally risky 15 year bonds is $10 \%$. The annual coupon rate for Bond $H$ is $10 \%$ and $B o n d L$ is $8 \%$.

What is the rate of change in each of the bond prices if market required rates fall to $8 \%$ ?

##  <br> Example of the Role of the Coupon Rate

The price on Bond $H$ and $L$ prior to the change in the market required rate of return is $\$ 1,000$ and $\$ 848$ respectively.

The price for Bond H will rise from $\mathbf{\$ 1 , 0 0 0}$ to \$1,171 (+17.1\%).

The price for Bond $L$ will rise from $\$ 848$ to \$1,000 (+17.9\%). Faster Increase!


## Determining the Yield on Preferred Stock

## Determine the yield for preferred stock with an infinite life.

$$
P_{0}=\operatorname{Div}_{P} / k_{P}
$$

Solving for $k_{p}$ such that

$$
\mathrm{k}_{\mathrm{P}}=\operatorname{Div}_{\mathrm{p}} I \mathrm{P}_{0}
$$



## Preferred Stock Yield Example

Assume that the annual dividend on each share of preferred stock is \$10. Each share of preferred stock is currently trading at $\$ 100$. What is the yield on preferred stock?

$$
\begin{gathered}
k_{p}=\$ 10 / \$ 100 . \\
k_{P}=10 \% .
\end{gathered}
$$

##  <br> Determining the Yield on Common Stock

Assume the constant growth model is appropriate. Determine the yield on the common stock.

$$
P_{0}=D_{1} I\left(k_{e}-g\right)
$$

Solving for $\mathrm{k}_{\mathrm{e}}$ such that

$$
k_{e}=\left(D_{1} / P_{0}\right)+g
$$



## Common Stock Yield Example

Assume that the expected dividend $\left(D_{1}\right)$ on each share of common stock is $\$ 3$. Each share of common stock is currently trading at $\$ 30$ and has an expected growth rate of $5 \%$. What is the yield on common stock?

$$
\begin{aligned}
& k_{\mathrm{e}}=(\$ 3 / \$ 30)+5 \% \\
& k_{e}=10 \%+5 \%=15 \%
\end{aligned}
$$

